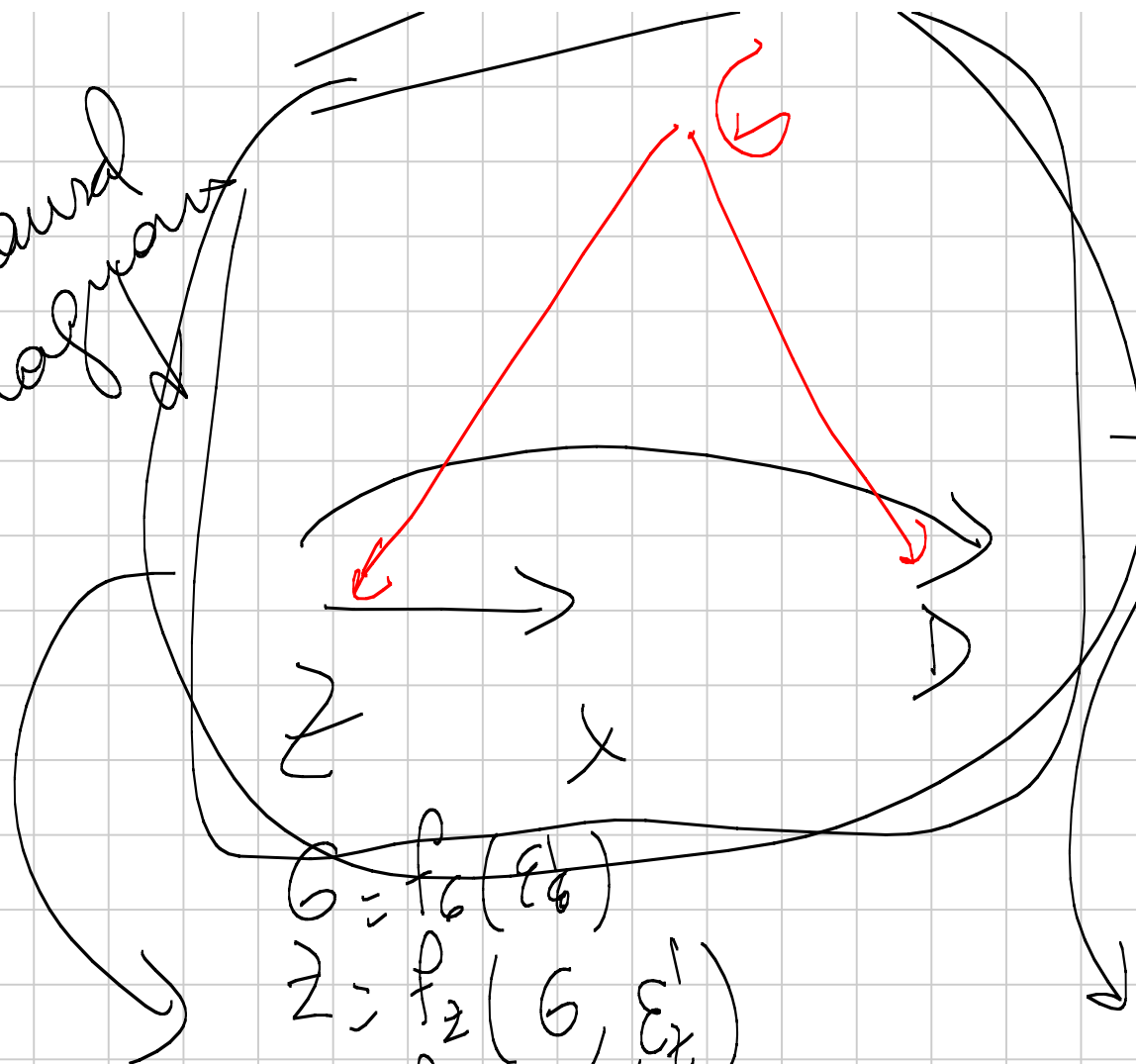
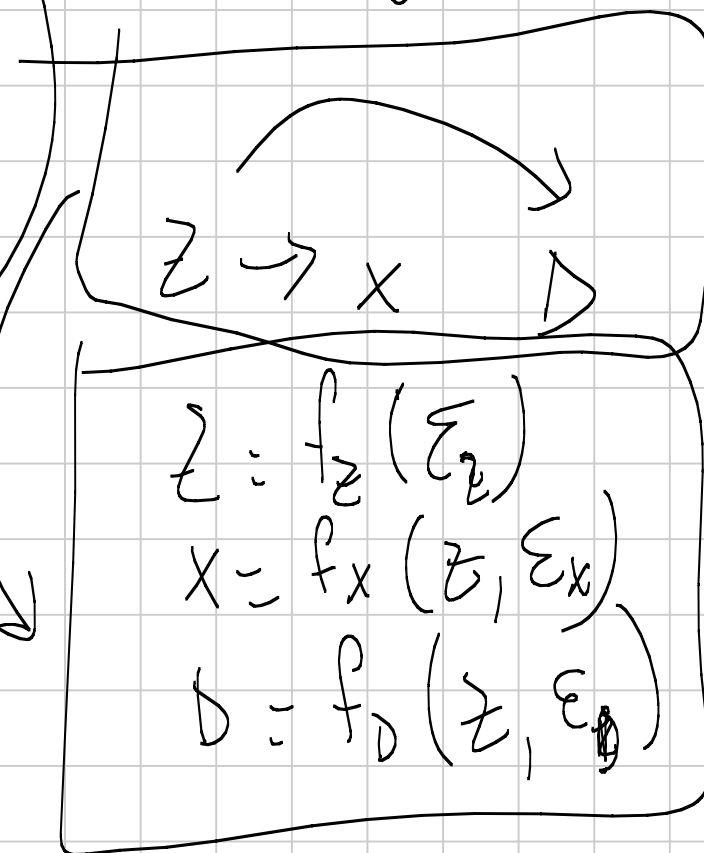


Causal diagram

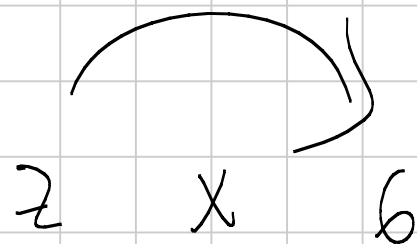
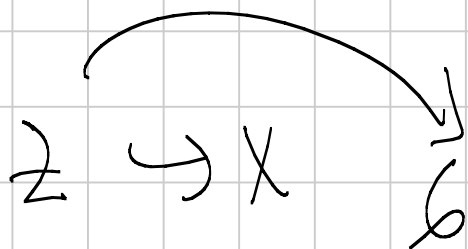


$$\begin{aligned} G &= f_G(\epsilon_G) \\ Z &= f_Z(G, \epsilon_Z) \\ X &= f_X(Z, \epsilon_X) \\ D &= f_D(G, Z, \epsilon_D) \end{aligned}$$

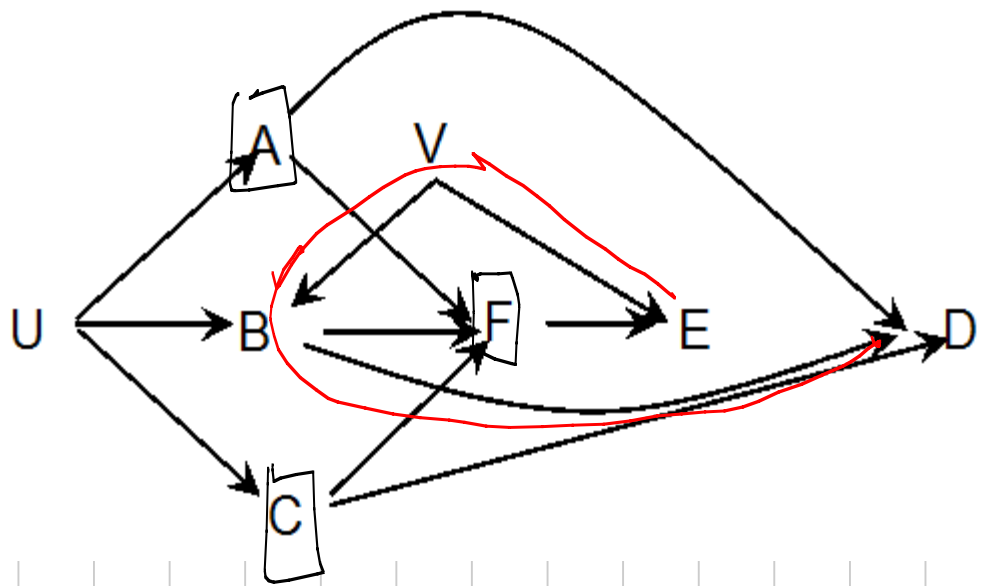
Not causal
↓
diag



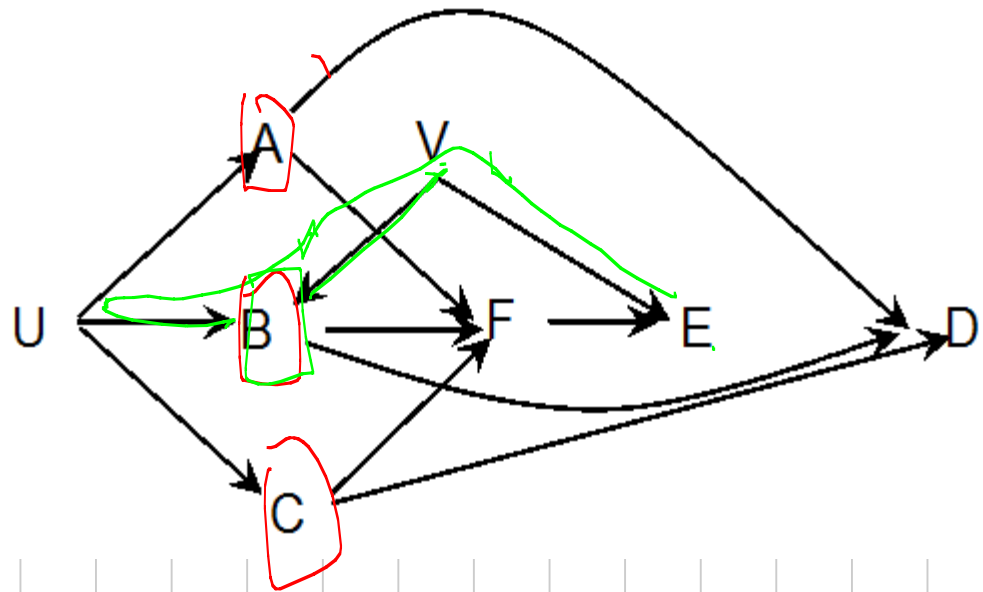
$$\begin{aligned} Z &= f_Z(\epsilon_Z) \\ X &= f_X(Z, \epsilon_X) \\ D &= f_D(Z, \epsilon_D) \end{aligned}$$

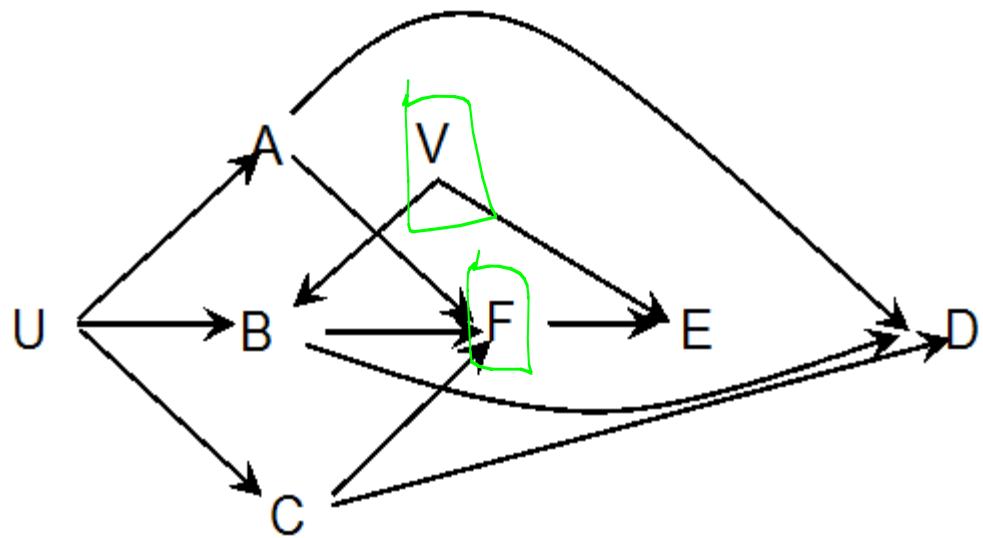


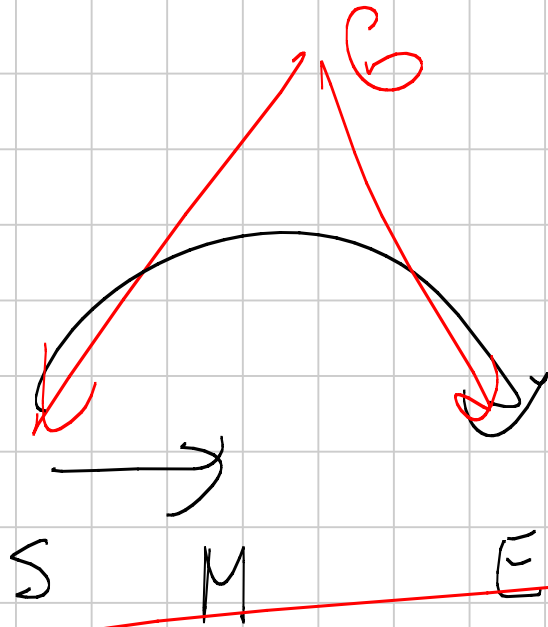
$$\begin{aligned} z &= f_z(\varepsilon_z) \\ X &= f_X(\varepsilon_X) \\ g &= f_g(z, \varepsilon_g) \end{aligned}$$



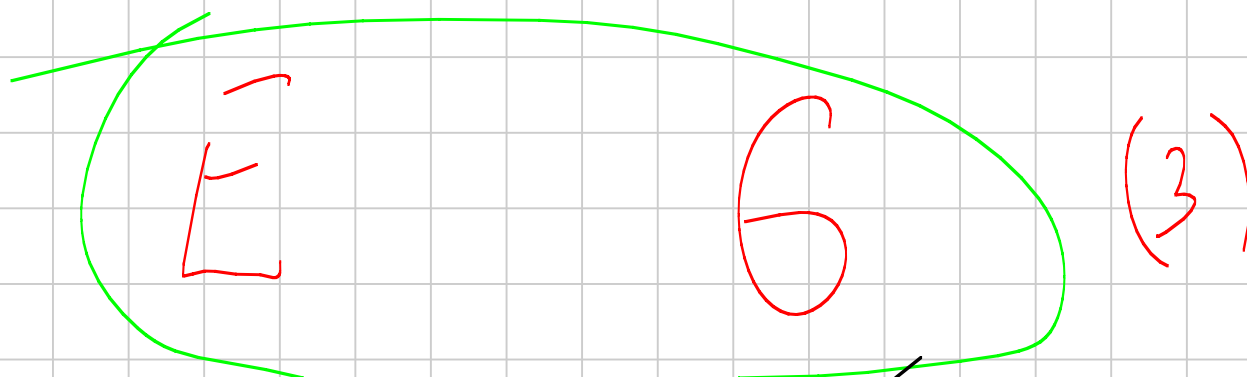
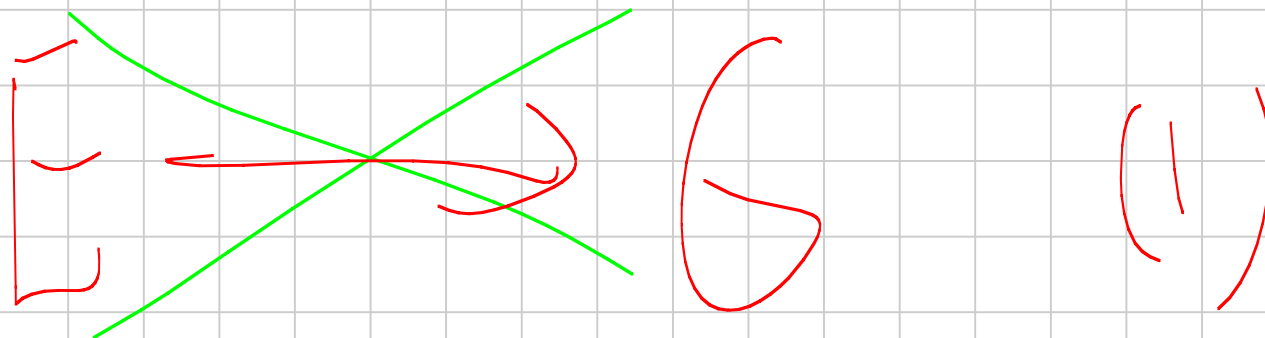
$(E \parallel D \mid A, C, F)_{\text{ag}}?$

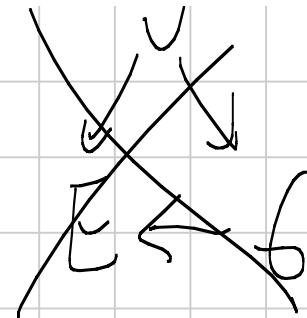
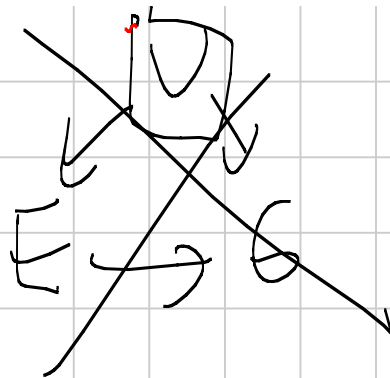
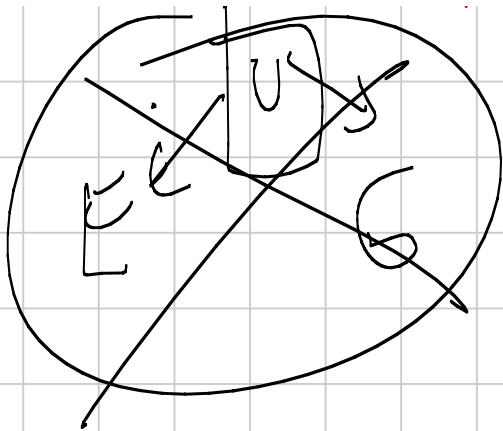






$$P(E_{S=1}=1) - P(E_{S=0}=1)$$





$E \quad G$

$E \rightarrow G$

$E \leftarrow G$

E and G are indep

$$E \perp\!\!\!\perp G \mid U$$

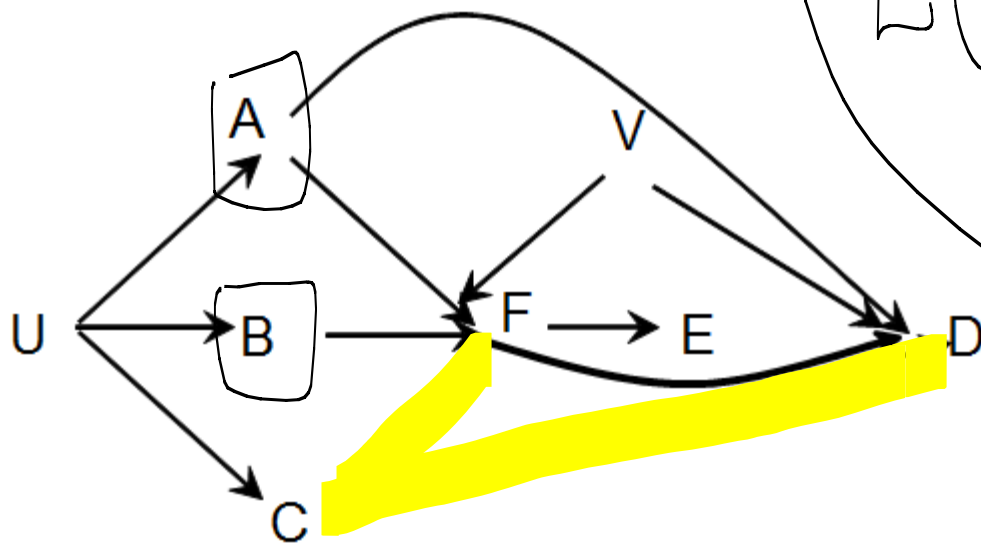
For all $(A \perp\!\!\!\perp Y \mid L)g$, L is a non-desc of A

$$\sum_{l=1}^5 P(L=l) P(Y_{i,1} = 1 \mid A=1, L=l) = \sum_l P(Y_{i,1} = 1 \mid L=l) P(L=l)$$

$$\sum_{l=1}^5 P(L=l) P(Y_{i,1} = 1 \mid A=1, L=l) = P(Y_{i,1} = 1)$$

C, A, B continuous

$$E(D | C=1) - E(D | C=0) \neq E(D_1) - E(D_0)$$



$$E(D_{C=c} | A, B) = E(D | C=c, A, B)$$

$$E(D_{C=1} | A, B) - E(D_{C=0} | A, B) =$$

$$E(D | C=1, A, B) - E(D | C=0, A, B)$$

$$E(D_c | A, B) = \beta_0 + \beta_1 C + \beta_2 A + \beta_3 B$$

$$+ \beta_4 C A + \dots$$

$$E(D | C, B, A) = \dots$$

